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Test Booklet Series

T.B.C. : PGT - 6/17



**TEST BOOKLET**

**PART - B**

**(MATHEMATICS)**

Serial No.

**6209**

**Time Allowed : 2 Hours**

**Maximum Marks : 100**

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10. Sheets for rough work are appended in the Test Booklet at the end.

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**SEAL**

1. The set of non-zero complex numbers form a group under :

- Addition
- Multiplication
- Addition as well as multiplication
- None of the above

2. If  $S$  is a subset of the finite group  $G$  under multiplication, then  $S$  is a subgroup of  $G$  if and only if  $S$  is nonempty and  $a, b \in S$  implies that :

- $ab \in S$
- $ab = 1$
- $ab^{-1} \in S$
- $ab^{-1}, a^{-1}b \in S$

3. The set of integers is a group under addition. The number of its elements of finite order are :

- None
- Infinite
- 1
- 2

4. An ideal  $P$  is a prime ideal, if :

- Order of  $P$  is prime
- $ab \in P \Rightarrow a, b \in P$
- $ab \in P \Rightarrow (a, b) \in 1$
- $ab \in P \Rightarrow$  either  $a \in P$  or  $b \in P$

5.  $M$  is a maximal ideal of the commutative ring  $R$  if and only if :

- $R/M$  is a normal subgroup
- $R \cap M$  is an ideal
- $R/M$  is a field
- $R \cap M$  is a proper ideal

6.  $X^2 + 1$  is the minimal polynomial of  $i$  over :

- Field  $R$  as well as  $Q$
- Field  $Q$  only
- Field of complex numbers only
- Neither  $R$  nor  $Q$

7. If  $f \in F[X]$  and degree of  $f$  is  $n$ , then  $f$  has a splitting field  $K$  over  $F$  with :

- $[K : F] < nl$
- $[K : F] < n$
- $[K : F] \leq nl$
- $[K : F] \leq n$

8. The number of primes not exceeding  $x$ , for indefinitely large  $x$ , can be approximated by :

- $\frac{x}{\log x}$
- $\frac{\exp x}{x}$
- $\frac{\coth x}{x}$
- $\frac{\cosh x}{x}$

9. For integers  $a, b & m$ ,  $a \equiv b \pmod{m}$   
 $\Rightarrow f(a) \equiv f(b) \pmod{m}$ , when  $f()$  is :

- A function over set of integers
- A polynomial
- A polynomial with Integer coefficients
- A continuous function

10. The number of solutions of  $5x + 3y = 52$  in positive integers are :

- Two
- Three
- Infinite
- Five

11. Let  $f(x)$  is continuous on  $[-1, 1]$ , then it is :

- Differentiable on  $[0, 1]$
- Differentiable at  $x = -1$  and  $x = 1$
- Uniformly continuous on  $[-1, 1]$
- Uniformly continuous on  $(-1, 1)$

12. Heine-Borel property ensures that :

- An open cover of a compact set has a finite sub-cover
- An open subset of a compact set has a bounded sub-cover
- Uniformly continuous function is differentiable.

13. A curve defined by mapping  $g : [a, b] \rightarrow \mathbb{R}^k$  is rectifiable, if  $g$  is :

- Continuous on  $[a, b]$
- Has derivative continuous on  $[a, b]$
- Is integrable on  $[a, b]$
- Is monotonically increasing

14. In a complete metric space :

- Every infinite series is convergent
- Every subset is compact
- Every function is closed
- Every Cauchy sequence is convergent

15. The value of integral  $\int_{-2\pi}^0 \sin^2 x dx$  is :

- 0
- $-\pi$
- $\pi/2$
- $-\pi/2$

16. The domain of function  $f(x) = \sin^{-1} [\log_2(x/2)]$  is :

- $[-1, 4]$
- $[1, -4]$
- $[1, 4]$
- None of the above

17. A function, uniformly continuous on an interval  $[a, b]$  :

- Is piecewise continuous on real line
- Is differentiable on  $[a, b]$
- Is Riemann integrable on  $[a, b]$
- Can be subjected to mean value theorem

18. A curve defined by mapping  $\gamma : [a, b] \rightarrow \mathbb{R}^k$  is called an arc, if :

- $\gamma(a) = \gamma(b)$
- $\gamma$  is one-one
- $\gamma$  is differentiable
- $\gamma$  is one-one and onto

19.  $f(x) = \frac{\sqrt{2} \cos x - 1}{\cot x - 1}$ , for  $x \neq \frac{\pi}{4}$ ; and  $f(x) = \alpha$ , at  $x = \frac{\pi}{4}$ . What should be the value of  $\alpha$  to make  $f(x)$  continuous at  $x = \frac{\pi}{4}$  ?

- $-\frac{1}{2}$
- $\sqrt{2}$
- $\frac{1}{2}$
- 2

20. The function  $f(x) = |x - 1| + |x - 2|$  is :

- Continuous at  $x = 1$  only
- Continuous at  $x = 1$  and  $x = 2$

(C) Differentiable at  $x = 1$  and  $x = 2$

(D) Not differentiable on  $(1, 2)$

21. Pole of a function is a point where the function becomes :

- Maximum
- Zero
- Unbounded
- Discontinuous

22. For a complex number  $z$ , the value of  $\sin^2 z + \cos^2 z$  is :

- $i$
- 1
- $1 + i$
- $1 - i$

23. Cauchy's residue theorem is used to solve :

- Initial value problems
- Boundary value problems
- Integral in complex domain
- Integral equations

24. Complex valued function  $f(z) = |z|^2$ , for complex  $z$ , is analytic :

- Nowhere in complex plane
- At  $z = 0$  only
- In entire complex plane
- In complex plane except at  $z = 0$

25. For analytic  $f(z) = u + iv$ , Cauchy-Riemann equations in polar coordinates are given by :

(A)  $u_r = v_\theta, u_\theta = -v_r$   
 (B)  $rv_r = u_\theta, v_\theta = -ru_r$   
 (C)  $u_r = v_r, u_\theta = -v_\theta$   
 (D)  $ru_r = v_\theta, u_\theta = -rv_r$

26. The complex valued function  $f(z) = u(x, y) + iv(x, y)$ , for  $z = x + iy$ , is analytic if and only if :

(A)  $v$  is derivative of  $u$   
 (B)  $v$  is integral of  $u$   
 (C)  $u$  and  $v$  are harmonic  
 (D)  $v$  is harmonic conjugate of  $u$

27. For  $z = x + iy$ ,  $x > 0$ , the integral  $\int_0^\infty e^{-zt} dt$  is equal to :

(A)  $z$   
 (B)  $\frac{1}{z}$   
 (C)  $\log z$   
 (D)  $e^{-z}$

28. Necessary condition for an arc  $z = z(t)$  ( $a \leq t \leq b$ ) to be smooth, is a :

(A) Continuous  $z'(t)$   
 (B) Integrable  $z(t)$   
 (C) Differentiable  $z(t)$   
 (D) Harmonic  $z(t)$

29. Residue of complex valued function  $z \cos\left(\frac{1}{z}\right)$  at  $z = 0$  is :

(A)  $-\frac{1}{4}$   
 (B)  $-\frac{1}{3}$   
 (C)  $-\frac{1}{2}$   
 (D)  $-1$

30. The transformation  $w = \frac{az + b}{cz + d}$  with complex constants  $a, b, c, d$  makes a bilinear transformation when :

(A)  $ad - bc = 0$   
 (B)  $ad - bc \neq 0$   
 (C)  $\frac{a}{d} = \frac{b}{c}$   
 (D)  $\frac{a}{d} = \frac{-b}{c}$

31. Which of the following shape does not make a convex region ?

(A) Rectangle  
 (B) Ellipse  
 (C) Triangle  
 (D) Star

32. Maximum value of  $2x_1 + 3x_2$  subject to the conditions  $x_1, x_2 \geq 0, x_1 - x_2 \leq 1, x_1 + x_2 \geq 3$  is :

(A) Infinite  
 (B) 15  
 (C) 28  
 (D) 65

33. An unbalanced assignment problem can be solved by converting into a balanced assignment problem by introducing dummy person or a dummy job with :

- Minimum Cost
- Maximum Cost
- Zero Cost
- Mean Cost

34. In VED classification to enhance the inventory control efficiency, alphabet D stands for :

- Demand
- Desirable
- Delivery
- Decoupling

35. EPQ model of inventory associates mainly with :

- Manufacturing environment
- Price discounts
- Larger consumption
- Cheaper transportation

36. A saddle point of a game is that place in the payoff matrix where :

- Minimum of the row maxima = minimum of the column maxima
- Maximum of the row minima = maximum of the column minima
- Maximum of the row minima = minimum of the column maxima
- Minimum of the row maxima = maximum of the column minima

37. The function to be maximized (or minimized) in linear programming procedure is called :

- Target function
- Optimised function
- Subjective function
- Objective function

38. The main basic function of inventory is to :

- Increase the manufacturing
- Increase the profitability
- Increase the consumption
- Construct the marketing support

39. If a standard problem and its dual are both feasible, then both are called :

- Bounded feasible
- Dual feasible
- Co-feasible
- Optimum feasible

40. Maximum of  $5x + 2y + z$  for  $x, y, z \geq 0$  and  $x + 3y - z \leq 6$ ;  $y + z \leq 4$ ;  $3x + y \leq 7$ , comes from

- $x = \frac{7}{3}, y = 1, z = 3$
- $x = \frac{1}{3}, y = 3, z = 0$
- $x = \frac{2}{3}, y = 3, z = 1$
- $x = \frac{7}{3}, y = 0, z = 4$

41. For Simpson rule to solve a definite integral, each section of the curve is replaced by :

- A secant chord
- A tangent to curve
- A second degree curve
- A spline arc

42. Gauss elimination method solves :

- A system of linear equations
- A cubic equation
- An algebraic equation of degree 4
- An integral equation

43. Gauss-Siedel method represents :

- A matrix inversion
- An iterative procedure
- An integral evaluation
- An interpolation technique

44. Newton-Raphson method is applied to solve :

- An algebraic equation
- A transcendental equation
- A system of simultaneous equations
- Any of these

45. Runge-Kutta methods are used to solve the differential equation of :

- Upto second order
- Upto order three

46. Cramer's rule is used to solve :

- An integral
- A system of linear equations
- An algebraic equation
- None of these

47. Jacobi's method requires the coefficient matrix in system of equations to be :

- Symmetric
- Hermitian
- Sparse
- Diagonally dominant

48. Order to convergence of secant method is approximately :

- 1.427
- 1.618
- 1.84
- 2.0

49. When performing Gaussian elimination, the pivot represents the :

- Largest element in column
- Largest element in row
- Largest element in matrix
- Diagonal element

50. Shooting method is used to solve :

- Any differential equation
- Only initial value problems
- Only boundary value problems
- System of differential equations

51. If a function  $f$  is measurable then :

- $|f|$  is always measurable
- $|f|$  is bounded but not measurable
- $f$  may be measurable subject to some conditions
- Then  $f$  should be a limit to sequence of functions

52. In the definition of Riemann-Stieltjes integral, given by  $\int_a^b f(x) d\alpha(x)$ , the function  $\alpha(x)$ ,  $x \in [a, b]$  must be a :

- Continuous function
- Monotonically decreasing function
- Monotonically increasing function
- Differentiable function

53. If  $f$  is a non-negative measurable function and  $\int_S f dm = 0$  then  $f$  is :

- A constant
- Zero everywhere
- A periodic function
- Zero, almost everywhere

54. For metric space  $X$  with metric  $d$ , the map  $\phi : X \rightarrow X$  is a contraction of  $X$ , if, for  $x, y \in X$  :

- $d(\phi(x), \phi(y)) \leq cd(x, y)$  with finite positive  $c$
- $d(\phi(x), \phi(y)) \leq cd(x, y)$  with real  $c \leq 1$
- $d(\phi(x), \phi(y)) \leq cd(x, y)$  with  $0 < c < 1$
- $d(\phi(x), \phi(y)) \leq cd(x, y)$  with real  $c < 1$

55. A real valued function defined on a measurable space is called a simple function if :

- The domain of the function is finite
- The range of the function is finite
- Measurable space is a vector space
- Function is a contraction map

56. The series  $\sum (n+1)^{1/3} - (n)^{1/3}$  is :

- Convergent
- Divergent
- Oscillatory
- A power series

57. If  $\{f_n\}$  is a monotone increasing sequence of non-negative measurable functions from  $S$  to  $\mathbb{R}$  then  $\int_S f dm = \lim_{n \rightarrow \infty} \int_S f_n dm$ . This theorem is known as :

- Bounded Convergence Theorem
- Dominated Convergence Theorem
- Monotone Convergence Theorem
- Monotone Measure Theorem

58. What is the length of an arc of the curve  $y = 1 - \ln(\cos x)$  intercepted between  $x = 0$  and  $x = \pi/4$  ?

(A)  $\ln(\sqrt{2} + 1)$   
 (B)  $\ln(\sqrt{2} + 2)$   
 (C)  $1 - \ln\sqrt{2}$   
 (D) None of these

59. The value of  $\int_0^{\pi/2} \sin x \log(\sin x) dx$  is :

(A)  $\log(\pi/2)$   
 (B)  $\log(e/2)$   
 (C)  $\log(2/\pi)$   
 (D)  $\log(2/e)$

60. The value of integral  $\int_{-1}^1 ([x] - x) dx$  is :

(A) -1  
 (B) 2  
 (C) 1  
 (D) 0

61. A norm on a vector space  $X$  is a function, whose range is a set of :

(A) Rational numbers  
 (B) Positive real numbers  
 (C) Real numbers  
 (D) Non-negative real numbers

62. According to Banach's criterion, a normed vector space  $X$  is complete if and only if every :

(A) Absolutely convergent series in  $X$  is convergent  
 (B) Convergent series in  $X$  is uniformly convergent  
 (C) Series in  $X$  is uniformly convergent  
 (D) Series in  $X$  is absolutely convergent

63. Given a vector space  $X$  with a subspace  $M$ . The codimension of  $M$  is the :

(A) g.c.d. of dimension of  $X$  and  $M$   
 (B) Number of functions from  $X$  to  $M$   
 (C) Dimension of quotient space  $X/M$   
 (D) Dimension of largest normed subspace of  $X$

64. A preorder  $\leq$  on a set is a binary relation that satisfies the properties of :

(A) Reflexivity  
 (B) Reflexivity and Transitivity  
 (C) Transitivity  
 (D) Symmetry and Reflexivity

65. A bounded (linear) operator from  $X$  to  $Y$  is a linear transformation  $T : X \rightarrow Y$  such that the operator norm  $\|T\|$  is :

(A) Finite  
 (B) Zero  
 (C) Infinite  
 (D) Unity

66. Let  $E$  and  $F$  are Banach spaces.  $T \in \mathcal{L}(E, F)$  becomes an open map when it is :

- (A) Bijective
- (B) Injective
- (C) Surjective
- (D) Neither injective nor surjective

67. Closed-graph theorem is used to give a proof of :

- (A) Open-mapping lemma
- (B) The principle of uniform boundedness
- (C) Urysohns lemma
- (D) Parseval's identity

68. Let  $(H, \langle \cdot, \cdot \rangle)$  be an inner product space, then for  $a, b \in H$ , the relation

$$\|x+y\|^2 + \|x-y\|^2 = 2\|x\|^2 + 2\|y\|^2$$

is known as :

- (A) Pythagorean theorem
- (B) Law of convexity
- (C) Reisz-Fischer theorem
- (D) Parallelogram Law

69. Let  $H$  be a separable Hilbert space. All orthonormal bases of  $H$  are :

- (A) Countable
- (B) Dense in  $H$
- (C) Proper closed subspaces
- (D) Separable

70. For an orthonormal subset  $\beta$  of  $H$ , which of the following are equivalent ?

- (1)  $\beta$  is a basis.
- (2)  $\beta$  is complete.
- (3)  $\text{Span } \beta = H$ .
- (A) (1) and (2)
- (B) (2) and (3)
- (C) (1) and (3)
- (D) All of these

71. Linear operator  $A$  on a finite-dimensional vector space  $X$  is one-to-one if and only if :

- (A) The range of  $A$  is all of  $X$
- (B) The domain of  $A$  is subset of  $X$
- (C) The domain and range of  $A$  is subset of  $X$
- (D) The domain of  $A$  is all of  $X$

72. If  $A$  is a  $n \times n$  non singular matrix, then  $\text{adj}(\text{adj } A)$  is equal to :

- (A)  $|A|^{n-2}$
- (B)  $|A|^{n-1}A$
- (C)  $|A|^{n-1}$
- (D)  $|A|^{n-2}A$

73. A square matrix  $A$  is singular if and only if its :

- (A) Columns are linearly independent
- (B) Rows are linearly independent
- (C) Columns are linearly dependent
- (D) Eigenvalues are non-zero

74. If  $\alpha$  is an eigenvalue of a nonsingular matrix  $A$  then corresponding eigenvalue of adjoint of  $A$  will be :

- $|A|\alpha$
- $|A|/\alpha$
- $|A|$
- $|A|^{-1}$

75. Of a square matrix, the product of its eigenvalues is equal to :

- Sum of its diagonal elements
- Product of its diagonal elements
- Its determinant
- Determinant of its adjoint

76. What value of  $k$  makes the vectors  $(1, -1, 3), (1, 2, -2), (k, 0, 1)$  linearly dependent ?

- $\frac{3}{4}$
- $\frac{1}{2}$
- $\frac{1}{4}$
- $-\frac{3}{4}$

77. Which of the following maps are linear transformations ?

- $T : \mathbb{R}^2 \rightarrow \mathbb{R}$  defined by  $T(x, y) = |2x - 3y|$
- $T : \mathbb{R}^2 \rightarrow \mathbb{R}$  defined by  $T(x, y) = xy$
- $T : \mathbb{R}^3 \rightarrow \mathbb{R}^2$  defined by  $T(x, y, z) = (z, x + y)$

78. The rank of  $T : \mathbb{R}^2 \rightarrow \mathbb{R}^3$ , defined as  $T(x, y) = (x + y, x - y, y)$ , is :

- 3
- 2
- 1
- 0

79. The eigenvalues for  $T : \mathbb{R}^3 \rightarrow \mathbb{R}^3$  defined by  $T(x, y, z) = (3x + y + 4z, 2y + 6z, 5z)$  are :

- 2, 3 and 5
- 3, 4 and 5
- 2, 3 and 4
- 1, 2 and 3

80. The dimension of the vector space  $C$  over the field of real numbers is :

- 1
- Infinite
- 2
- 4

81. Let  $p$  denotes the statement "Rahul is rich" and  $q$  denotes the statement "Rahul is happy". Then the statement "Rahul is poor or he is both rich and unhappy" is expressed as :

(A)  $\sim p \vee (p \wedge \sim q)$   
 (B)  $p \vee (p \wedge \sim q)$   
 (C)  $\sim p \vee (p \wedge q)$   
 (D)  $p \vee (p \wedge q)$

82. In terms of  $\downarrow$ ,  $p \rightarrow q$  is expressed as :

(A)  $(p \downarrow q) \downarrow (q \downarrow p)$   
 (B)  $(\sim p \downarrow q) \downarrow (\sim q \downarrow p)$   
 (C)  $(\sim p \downarrow q) \downarrow (\sim p \downarrow q)$   
 (D)  $(p \downarrow q) \downarrow (p \downarrow q)$

83. A poset  $(L, \leq)$  becomes a lattice when every non-empty finite subset of  $L$  has :

(A) A supremum  
 (B) An infimum  
 (C) A supremum as well as an infimum  
 (D) Neither supremum nor infimum

84. In the lattice  $L = \{1, 2, 3, 5, 6, 10, 15, 30\}$  ordered by divisibility, the atoms are :

(A) 1, 2, 3, 5  
 (B) 2, 3, 5  
 (C) 1, 2, 3  
 (D) 3, 5

85. In recurrence relation  $a_{r+2} = 2a_{r+1} + a_r$ ,  $a_0 = 2$ ,  $a_1 = 1$ , the  $a_r$  is given by :

(A)  $1 + 2r + 2^r$   
 (B)  $1 + 2r - 2^r$   
 (C)  $1 - 2r - 2^r$   
 (D)  $1 - 2r + 2^r$

86. The dual of  $a + a'b = a + b$  is :

(A)  $a(a' + b) = ab$   
 (B)  $a(a' + b) = a'b$   
 (C)  $a(a + b) = ab$   
 (D)  $a'(a + b) = ab$

87. For every pair of elements  $a$  and  $b$ , DeMorgan's laws in Boolean algebra are :

(A)  $(a + b)' = a' + b' \& (a * b)' = a' * b'$   
 (B)  $(a + b)' = b' + a' \& (a * b)' = b * a$   
 (C)  $(a + b)' = a' * b' \& (a * b)' = a' + b'$   
 (D)  $(a + b)' = a * b \& (a * b)' = a + b$

88. In minimal form, the function  $f(x, y, z) = xyz + xy'z + x'yz + x'y'z$  is written as :

(A)  $f = z'$   
 (B)  $f = z$   
 (C)  $f = x + z$   
 (D)  $f = y + z$

89. Let a simple graph of 15 edges, 3 vertices of degree 4 and all other vertices of degree 3. The number of edges in this graph are :

(A) 6  
(B) 8  
(C) 9  
(D) 10

90. Nullity of a complete graph of 7 vertices is :

(A) 7  
(B) 8  
(C) 14  
(D) 21

91. Frobenius' method is used to find the power series solution of :

(A) Integral equations  
(B) Ordinary differential equations with variable coefficients  
(C) Partial differential equations  
(D) Integro-differential equations

92. The differential equation  $(1 - x^2) \frac{d^2y}{dx^2} - 2x \frac{dy}{dx} + m(m + 1)y = 0$  is known as :

(A) Bessel's equation

(B) Hermite's equation  
(C) Kelvin's equation  
(D) Legendre's equation

93. For  $J_n(x)$  being Bessel's function of first kind,  $\frac{d}{dx} [x^n J_n(x)]$  is equal to :

(A)  $x^n J_{n+1}(x)$   
(B)  $x^{n-1} J_{n+1}(x)$   
(C)  $x^n J_{n-1}(x)$   
(D)  $x^{n-1} J_n(x)$

94. For  $x \rightarrow 0$ ,  $J_n(x)$  is approximated as :

(A)  $\frac{1}{\Gamma(n+1)} \left(\frac{x}{2}\right)^n$   
(B)  $\frac{1}{\Gamma(n)} \left(\frac{x}{2}\right)^n$   
(C)  $\frac{1}{\Gamma(n+1)} x^n$   
(D)  $\frac{1}{\Gamma(n)} x^n$

95. Heat conduction equation is classified as :

(A) Hyperbolic equation  
(B) Parabolic equation  
(C) Elliptic equation  
(D) Harmonic equation

96. Laplace transform of  $\frac{\sin ht}{t}$  is :

(A)  $\frac{1}{2} \log\left(\frac{s-1}{s+1}\right)$

(B)  $\frac{1}{2} \log\left(\frac{s+1}{s-1}\right)$

(C)  $-\frac{1}{2} \log\left(\frac{s-1}{s+1}\right)$

(D)  $-\frac{1}{2} \log\left(\frac{s+1}{s-1}\right)$

97. Inverse Laplace transform of  $\frac{1}{2s-5}$  is :

(A)  $\frac{1}{2} \exp\left(\frac{3}{2}t\right)$

(B)  $\frac{5}{2} \exp\left(\frac{1}{3}t\right)$

(C)  $\frac{2}{5} \exp\left(\frac{3}{2}t\right)$

(D)  $\frac{1}{3} \exp\left(\frac{5}{2}t\right)$

98. For a function, given by  $f(x) = 1$  for  $|x| < a$  but  $f(x) = 0$  for  $|x| > a$ , the Fourier transform is given by :

(A)  $\frac{1}{s} \cos(sa)$

(B)  $\frac{2}{s} \sin(sa)$

(C)  $\frac{1}{a} \cos(sa)$

(D)  $\frac{2}{a} \sin(sa)$

99. If  $f(s)$  denotes the Fourier transform of  $F(x)$ , then the Fourier transform of  $F(ax)$  is given by :

(A)  $af\left(\frac{s}{a}\right)$

(B)  $\frac{1}{a} f(sa)$

(C)  $af(sa)$

(D)  $\frac{1}{a} f\left(\frac{s}{a}\right)$

100. The equation  $\frac{\partial^2 u}{\partial x^2} + i \frac{\partial u}{\partial t} = 0$ , is known as :

(A) Burger's equation

(B) Transport equation

(C) Schrodinger's equation

(D) Maxwell's equation

**SPACE FOR ROUGH WORK**



QS - 6A/6

( 15 )

( Turn over )

**SPACE FOR ROUGH WORK**

**SEAL**



QS – 6A/6 (75)

( 16 )

Part – B (Mathematics)