



Teachingninja.in



Latest Govt Job updates



Private Job updates



Free Mock tests available

Visit - teachingninja.in



GATE
Previous Year Paper
Mathematics 2020





MA: Mathematics

GA - General Aptitude

Q1 - Q5 carry one mark each.

Q.No. 1 Rajiv Gandhi Khel Ratna Award was conferred_____Mary Kom, a six-time world champion in boxing, recently in a ceremony_____the Rashtrapati Bhawan (the President's official residence) in New Delhi.

- (A) with, at
- (B) on, in
- (C) on, at
- (D) to, at

Q.No. 2 Despite a string of poor performances, the chances of K. L. Rahul's selection in the team are_____.

- (A) slim
- (B) bright
- (C) obvious
- (D) uncertain

Q.No. 3 Select the word that fits the analogy:

Cover : Uncover :: Associate : _____

- (A) Unassociate
- (B) Inassociate
- (C) Misassociate
- (D) Dissociate

Q.No. 4 Hit by floods, the kharif (summer sown) crops in various parts of the country have been affected. Officials believe that the loss in production of the kharif crops can be recovered in the output of the rabi (winter sown) crops so that the country can achieve its food-grain production target of 291 million tons in the crop year 2019-20 (July-June). They are hopeful that good rains in July-August will help the soil retain moisture for a longer period, helping winter sown crops such as wheat and pulses during the November-February period.

Which of the following statements can be inferred from the given passage?

- (A) Officials declared that the food-grain production target will be met due to good rains.
- (B) Officials want the food-grain production target to be met by the November-February period.
- (C) Officials feel that the food-grain production target cannot be met due to floods.
- (D) Officials hope that the food-grain production target will be met due to a good rabi produce.

Q.No. 5 The difference between the sum of the first $2n$ natural numbers and the sum of the first n odd natural numbers is _____.

- (A) $n^2 - n$
- (B) $n^2 + n$
- (C) $2n^2 - n$

- (D) $2n^2 + n$

Q6 - Q10 carry two marks each.

- Q.No. 6 Repo rate is the rate at which Reserve Bank of India (RBI) lends commercial banks, and reverse repo rate is the rate at which RBI borrows money from commercial banks.

Which of the following statements can be inferred from the above passage?

- (A) Decrease in repo rate will increase cost of borrowing and decrease lending by commercial banks.
(B) Increase in repo rate will decrease cost of borrowing and increase lending by commercial banks.
(C) Increase in repo rate will decrease cost of borrowing and decrease lending by commercial banks.
(D) Decrease in repo rate will decrease cost of borrowing and increase lending by commercial banks.

- Q.No. 7 P, Q, R, S, T, U, V, and W are seated around a circular table.

- I. S is seated opposite to W.
II. U is seated at the second place to the right of R.
III. T is seated at the third place to the left of R.
IV. V is a neighbour of S.

Which of the following must be true?

- (A) P is a neighbour of R.
(B) Q is a neighbour of R.
(C) P is not seated opposite to Q.
(D) R is the left neighbour of S.

- Q.No. 8 The distance between Delhi and Agra is 233 km. A car P started travelling from Delhi to Agra and another car Q started from Agra to Delhi along the same road 1 hour after the car P started. The two cars crossed each other 75 minutes after the car Q started. Both cars were travelling at constant speed. The speed of car P was 10 km/hr more than the speed of car Q . How many kilometers the car Q had travelled when the cars crossed each other?

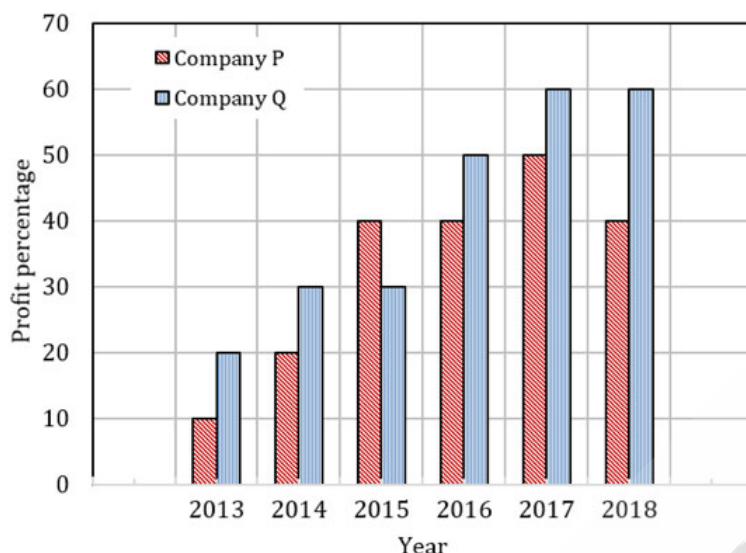
- (A) 66.6
(B) 75.2
(C) 88.2
(D) 116.5

- Q.No. 9 For a matrix $M = [m_{ij}]$; $i, j = 1, 2, 3, 4$, the diagonal elements are all zero and $m_{ij} = -m_{ji}$. The minimum number of elements required to fully specify the matrix is _____.

- (A) 0
(B) 6
(C) 12
(D) 16

- Q.No. 10

The profit shares of two companies P and Q are shown in the figure. If the two companies have invested a fixed and equal amount every year, then the ratio of the total revenue of company P to the total revenue of company Q, during 2013 - 2018 is _____.



- (A) 15 : 17
- (B) 16 : 17
- (C) 17 : 15
- (D) 17 : 16

MA: Mathematics

Q1 - Q25 carry one mark each.

Q.No. 1 Suppose that \mathfrak{T}_1 and \mathfrak{T}_2 are topologies on X induced by metrics d_1 and d_2 , respectively, such that $\mathfrak{T}_1 \subseteq \mathfrak{T}_2$. Then which of the following statements is TRUE?

- (A) If a sequence converges in (X, d_2) then it converges in (X, d_1)
- (B) If a sequence converges in (X, d_1) then it converges in (X, d_2)
- (C) Every open ball in (X, d_1) is an open ball in (X, d_2)
- (D) The map $x \mapsto x$ from (X, d_1) to (X, d_2) is continuous

Q.No. 2 Let $D = [-1, 1] \times [-1, 1]$. If the function $f: D \rightarrow \mathbb{R}$ is defined by

$$f(x, y) = \begin{cases} \frac{x^2 - y^2}{(x^2 + y^2)^2}, & (x, y) \neq (0, 0) \\ 0, & (x, y) = (0, 0) \end{cases},$$

then

- (A) f is continuous at $(0, 0)$
- (B) both the first order partial derivatives of f exist at $(0, 0)$
- (C) $\iint_D |f(x, y)|^{\frac{1}{2}} dx dy$ is finite
- (D) $\iint_D |f(x, y)| dx dy$ is finite

Q.No. 3 The initial value problem

$$y' = y^{\frac{3}{5}}, \quad y(0) = b$$

has

- (A)

- a unique solution if $b = 0$
- (B) no solution if $b = 1$
- (C) infinitely many solutions if $b = 2$
- (D) a unique solution if $b = 1$

Q.No. 4 Consider the following statements:

I : $\log(|z|)$ is harmonic on $\mathbb{C} \setminus \{0\}$

II : $\log(|z|)$ has a harmonic conjugate on $\mathbb{C} \setminus \{0\}$

Then

- (A) both I and II are true
- (B) I is true but II is false
- (C) I is false but II is true
- (D) both I and II are false

Q.No. 5 Let G and H be defined by

$$G = \mathbb{C} \setminus \{z = x + iy \in \mathbb{C} : x \leq 0, y = 0\},$$

$$H = \mathbb{C} \setminus \{z = x + iy \in \mathbb{C} : x \in \mathbb{Z}, x \leq 0, y = 0\}.$$

Suppose $f: G \rightarrow \mathbb{C}$ and $g: H \rightarrow \mathbb{C}$ are analytic functions. Consider the following statements:

I : $\int_{\gamma} f dz$ is independent of paths γ in G joining $-i$ and i

II : $\int_{\gamma} g dz$ is independent of paths γ in H joining $-i$ and i

Then

- (A) both I and II are true
- (B) I is true but II is false
- (C) I is false but II is true
- (D) both I and II are false

Q.No. 6 Let $f(z) = e^{1/z}$, $z \in \mathbb{C} \setminus \{0\}$ and let, for $n \in \mathbb{N}$,

$$R_n = \left\{ z = x + iy \in \mathbb{C} : |x| < \frac{1}{n}, |y| < \frac{1}{n} \right\} \setminus \{0\}.$$

If for a subset S of \mathbb{C} , \bar{S} denotes the closure of S in \mathbb{C} , then

- (A) $\overline{f(R_{n+1})} \neq f(R_n)$
- (B) $\overline{f(R_n) \setminus f(R_{n+1})} = \overline{f(R_n \setminus R_{n+1})}$
- (C) $\overline{f(\cap_{n=1}^{\infty} R_n)} = \cap_{n=1}^{\infty} \overline{f(R_n)}$
- (D) $\overline{f(R_n)} = \overline{f(R_{n+1})}$

Q.No. 7

Suppose that

$$U = \mathbb{R}^2 \setminus \{(x, y) \in \mathbb{R}^2 : x, y \in \mathbb{Q}\},$$

$$V = \mathbb{R}^2 \setminus \left\{ (x, y) \in \mathbb{R}^2 : x > 0, y = \frac{1}{x} \right\}.$$

Then, with respect to the Euclidean metric on \mathbb{R}^2 ,

- (A) both U and V are disconnected
- (B) U is disconnected but V is connected
- (C) U is connected but V is disconnected
- (D) both U and V are connected

Q.No. 8 If (D1) and (D2) denote the dual problems of the linear programming problems (P1) and (P2), respectively, where

(P1) : minimize $x_1 - 2x_2$ subject to $-x_1 + x_2 = 10, x_1, x_2 \geq 0$,

(P2) : minimize $x_1 - 2x_2$ subject to $-x_1 + x_2 = 10, x_1 - x_2 = 10, x_1, x_2 \geq 0$,

then

- (A) both (D1) and (D2) are infeasible
- (B) (P2) is infeasible and (D2) is feasible
- (C) (D1) is infeasible and (D2) is feasible but unbounded
- (D) (P1) is feasible but unbounded and (D1) is feasible

Q.No. 9 If $(4, 0)$ and $(0, -\frac{1}{2})$ are critical points of the function

$$f(x, y) = 5 - (\alpha + \beta)x^2 + \beta y^2 + (\alpha + 1)y^3 + x^3,$$

where $\alpha, \beta \in \mathbb{R}$, then

- (A) $(4, -\frac{1}{2})$ is a point of local maxima of f
- (B) $(4, -\frac{1}{2})$ is a saddle point of f
- (C) $\alpha = 4, \beta = 2$
- (D) $(4, -\frac{1}{2})$ is a point of local minima of f

Q.No. 10 Consider the iterative scheme

$$x_n = \frac{x_{n-1}}{2} + \frac{3}{x_{n-1}}, \quad n \geq 1,$$

with initial point $x_0 > 0$. Then the sequence $\{x_n\}$

- (A) converges only if $x_0 > 1$
- (B) converges only if $x_0 < 3$
- (C) converges for any x_0
- (D) does not converge for any x_0

Q.No. 11

Let $C[0, 1]$ denote the space of all real-valued continuous functions on $[0, 1]$ equipped with the supremum norm $\|\cdot\|_\infty$. Let $T: C[0, 1] \rightarrow C[0, 1]$ be the linear operator defined by

$$T(f)(x) = \int_0^x e^{-y} f(y) dy.$$

Then

- (A) $\|T\| = 1$
- (B) $I - T$ is not invertible
- (C) T is surjective
- (D) $\|I + T\| = 1 + \|T\|$

Q.No. 12 Suppose that M is a 5×5 matrix with real entries and $p(x) = \det(xI - M)$. Then

- (A) $p(0) = \det(M)$
- (B) every eigenvalue of M is real if $p(1) + p(2) = 0 = p(2) + p(3)$
- (C) M^{-1} is necessarily a polynomial in M of degree 4 if M is invertible
- (D) M is not invertible if $M^2 - 2M = 0$

Q.No. 13 Let $C[0, 1]$ denote the space of all real-valued continuous functions on $[0, 1]$ equipped with the supremum norm $\|\cdot\|_\infty$. Let $f \in C[0, 1]$ be such that

$$|f(x) - f(y)| \leq M|x - y|, \text{ for all } x, y \in [0, 1] \text{ and for some } M > 0.$$

For $n \in \mathbb{N}$, let $f_n(x) = f\left(x^{1+\frac{1}{n}}\right)$. If $S = \{f_n : n \in \mathbb{N}\}$, then

- (A) the closure of S is compact
- (B) S is closed and bounded
- (C) S is bounded but not totally bounded
- (D) S is compact

Q.No. 14 Let $K : \mathbb{R} \times (0, \infty) \rightarrow \mathbb{R}$ be a function such that the solution of the initial value problem $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$, $u(x, 0) = f(x)$, $x \in \mathbb{R}$, $t > 0$, is given by

$$u(x, t) = \int_{\mathbb{R}} K(x - y, t) f(y) dy$$

for all bounded continuous functions f . Then the value of $\int_{\mathbb{R}} K(x, t) dx$ is _____

Q.No. 15 The number of cyclic subgroups of the quaternion group

$$Q_8 = \langle a, b \mid a^4 = 1, a^2 = b^2, ba = a^3b \rangle$$

is _____

Q.No. 16 The number of elements of order 3 in the symmetric group S_6 is _____

Q.No. 17 Let F be the field with 4096 elements. The number of proper subfields of F is _____

Q.No. 18 If (x_1^*, x_2^*) is an optimal solution of the linear programming problem,

minimize $x_1 + 2x_2$
subject to

$$\begin{aligned} 4x_1 - x_2 &\geq 8 \\ 2x_1 + x_2 &\geq 10 \\ -x_1 + x_2 &\leq 7 \\ x_1, x_2 &\geq 0 \end{aligned}$$

and $(\lambda_1^*, \lambda_2^*, \lambda_3^*)$ is an optimal solution of its dual problem, then $\sum_{i=1}^2 x_i^* + \sum_{j=1}^3 \lambda_j^*$ is equal to _____ (correct up to one decimal place)

Q.No. 19 Let $a, b, c \in \mathbb{R}$ be such that the quadrature rule

$$\int_{-1}^1 f(x) dx \approx af(-1) + bf(0) + cf'(1)$$

is exact for all polynomials of degree less than or equal to 2. Then b is equal to _____ (rounded off to two decimal places)

Q.No. 20 Let $f(x) = x^4$ and let $p(x)$ be the interpolating polynomial of f at nodes 1, 2 and 3. Then $p(0)$ is equal to _____

Q.No. 21 For $n \geq 2$, define the sequence $\{x_n\}$ by

$$x_n = \frac{1}{2\pi} \int_0^{\frac{\pi}{2}} \tan^{\frac{1}{n}} t \, dt.$$

Then the sequence $\{x_n\}$ converges to _____ (correct up to two decimal places)

Q.No. 22 Let

$$L^2[0, 10] = \left\{ f: [0, 10] \rightarrow \mathbb{R} : f \text{ is Lebesgue measurable and } \int_0^{10} f^2 dx < \infty \right\}$$

equipped with the norm $\|f\| = \left(\int_0^{10} f^2 dx \right)^{\frac{1}{2}}$ and let T be the linear functional on $L^2[0, 10]$ given by

$$T(f) = \int_0^2 f(x) dx - \int_3^{10} f(x) dx.$$

Then $\|T\|$ is equal to _____

Q.No. 23

If $\{x_{13}, x_{22}, x_{23} = 10, x_{31}, x_{32}, x_{34}\}$ is the set of basic variables of a balanced transportation problem seeking to minimize cost of transportation from origins to destinations, where the cost matrix is,

	D_1	D_2	D_3	D_4	Availability
O_1	6	2	-1	0	10
O_2	4	2	2	3	$\lambda+5$
O_3	3	1	2	1	3λ
Demand	10	$\mu - 5$	$\mu + 5$	15	

and $\lambda, \mu \in \mathbb{R}$, then x_{32} is equal to _____

Q.No. 24 Let \mathbb{Z}_{225} be the ring of integers modulo 225. If x is the number of prime ideals and y is the number of nontrivial units in \mathbb{Z}_{225} , then $x + y$ is equal to _____

Q.No. 25 Let $u(x, t)$ be the solution of

$$\frac{\partial^2 u}{\partial t^2} - \frac{\partial^2 u}{\partial x^2} = 0, \quad u(x, 0) = f(x), \quad \frac{\partial u}{\partial t}(x, 0) = 0, \quad x \in \mathbb{R}, t > 0,$$

where f is a twice continuously differentiable function. If $f(-2) = 4, f(0) = 0$, and $u(2, 2) = 8$, then the value of $u(1, 3)$ is _____

Q26 - Q55 carry two marks each.

Q.No. 26 Let $\{e_n\}_{n=1}^\infty$ be an orthonormal basis for a separable Hilbert space H with the inner product $\langle \cdot, \cdot \rangle$. Define

$$f_n = e_n - \frac{1}{n+1} e_{n+1} \text{ for } n \in \mathbb{N}.$$

Then

- (A) the closure of the span $\{f_n; n \in \mathbb{N}\}$ equals H
- (B) $f = 0$ if $\langle f, f_n \rangle = \langle f, e_n \rangle$ for all $n \in \mathbb{N}$
- (C) $\{f_n\}_{n=1}^\infty$ is an orthogonal subset of H
- (D) there does not exist nonzero $f \in H$ such that $\langle f, e_2 \rangle = \langle f, f_2 \rangle$

Q.No. 27 Suppose V is a finite dimensional non-zero vector space over \mathbb{C} and $T: V \rightarrow V$ is a linear transformation such that $\text{Range}(T) = \text{Nullspace}(T)$. Then which of the following statements is FALSE?

- (A) The dimension of V is even
- (B) 0 is the only eigenvalue of T
- (C) Both 0 and 1 are eigenvalues of T
- (D) $T^2 = 0$

Q.No. 28

Let $P \in M_{m \times n}(\mathbb{R})$. Consider the following statements:

I : If $XPY = 0$ for all $X \in M_{1 \times m}(\mathbb{R})$ and $Y \in M_{n \times 1}(\mathbb{R})$, then $P = 0$.

II : If $m = n$, P is symmetric and $P^2 = 0$, then $P = 0$.

Then

- (A) both I and II are true
- (B) I is true but II is false
- (C) I is false but II is true
- (D) both I and II are false

Q.No. 29 For $n \in \mathbb{N}$, let $T_n: (l^1, \|\cdot\|_1) \rightarrow (l^\infty, \|\cdot\|_\infty)$ and $T: (l^1, \|\cdot\|_1) \rightarrow (l^\infty, \|\cdot\|_\infty)$ be the bounded linear operators defined by

$$T_n(x_1, x_2, \dots) = (y_1, y_2, \dots), \text{ where } y_j = \begin{cases} x_j, & j \leq n \\ x_n, & j > n \end{cases}$$

and

$$T(x_1, x_2, \dots) = (x_1, x_2, \dots).$$

Then

- (A) $\|T_n\|$ does not converge to $\|T\|$ as $n \rightarrow \infty$
- (B) $\|T_n - T\|$ converges to zero as $n \rightarrow \infty$
- (C) for all $x \in l^1$, $\|T_n(x) - T(x)\|$ converges to zero as $n \rightarrow \infty$
- (D) for each non-zero $x \in l^1$, there exists a continuous linear functional g on l^∞ such that $g(T_n(x))$ does not converge to $g(T(x))$ as $n \rightarrow \infty$

Q.No. 30 Let $P(\mathbb{R})$ denote the power set of \mathbb{R} , equipped with the metric

$$d(U, V) = \sup_{x \in \mathbb{R}} |\chi_U(x) - \chi_V(x)|,$$

where χ_U and χ_V denote the characteristic functions of the subsets U and V , respectively, of \mathbb{R} . The set $\{ \{m\} : m \in \mathbb{Z} \}$ in the metric space $(P(\mathbb{R}), d)$ is

- (A) bounded but not totally bounded
- (B) totally bounded but not compact
- (C) compact
- (D) not bounded

Q.No. 31 Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by

$$f(x) = \sum_{n=0}^{\infty} \frac{1}{2^n} \chi_{(n, n+1]}(x),$$

where $\chi_{(n, n+1]}$ is the characteristic function of the interval $(n, n+1]$. For $\alpha \in \mathbb{R}$, let $S_\alpha = \{x \in \mathbb{R} : f(x) > \alpha\}$. Then

- (A) $S_{\frac{1}{2}}$ is open
- (B) $S_{\frac{\sqrt{5}}{2}}$ is not measurable
- (C) S_0 is closed

(D) $S_{\frac{1}{\sqrt{2}}}$ is measurable

Q.No. 32 For $n \in \mathbb{N}$, let $f_n, g_n: (0, 1) \rightarrow \mathbb{R}$ be functions defined by

$$f_n(x) = x^n \text{ and } g_n(x) = x^n(1 - x).$$

Then

- (A) $\{f_n\}$ converges uniformly but $\{g_n\}$ does not converge uniformly
- (B) $\{g_n\}$ converges uniformly but $\{f_n\}$ does not converge uniformly
- (C) both $\{f_n\}$ and $\{g_n\}$ converge uniformly
- (D) neither $\{f_n\}$ nor $\{g_n\}$ converge uniformly

Q.No. 33 Let u be a solution of the differential equation $y' + xy = 0$ and let $\phi = u\psi$ be a solution of the differential equation $y'' + 2xy' + (x^2 + 2)y = 0$ satisfying $\phi(0) = 1$ and $\phi'(0) = 0$. Then $\phi(x)$ is

- (A) $(\cos^2 x)e^{-\frac{x^2}{2}}$
- (B) $(\cos x)e^{-\frac{x^2}{2}}$
- (C) $(1 + x^2)e^{-\frac{x^2}{2}}$
- (D) $(\cos x)e^{-x^2}$

Q.No. 34 For $n \in \mathbb{N} \cup \{0\}$, let y_n be a solution of the differential equation

$$xy'' + (1 - x)y' + ny = 0$$

satisfying $y_n(0) = 1$. For which of the following functions $w(x)$, the integral

$$\int_0^\infty y_p(x) y_q(x) w(x) dx, \quad (p \neq q)$$

is equal to zero?

- (A) e^{-x^2}
- (B) e^{-x}
- (C) xe^{-x^2}
- (D) xe^{-x}

Q.No. 35

Suppose that

$$X = \{(0,0)\} \cup \left\{ \left(x, \sin \frac{1}{x}\right) : x \in \mathbb{R} \setminus \{0\} \right\}$$

and

$$Y = \{(0,0)\} \cup \left\{ \left(x, x \sin \frac{1}{x}\right) : x \in \mathbb{R} \setminus \{0\} \right\}$$

are metric spaces with metrics induced by the Euclidean metric of \mathbb{R}^2 . Let B_X and B_Y be the open unit balls around $(0,0)$ in X and Y , respectively. Consider the following statements:

I : The closure of B_X in X is compact.

II : The closure of B_Y in Y is compact.

Then

- (A) both I and II are true
- (B) I is true but II is false
- (C) I is false but II is true
- (D) both I and II are false

Q.No. 36 If $f: \mathbb{C} \setminus \{0\} \rightarrow \mathbb{C}$ is a function such that $f(z) = f\left(\frac{z}{|z|}\right)$ and its restriction to the unit circle is continuous, then

- (A) f is continuous but not necessarily analytic
- (B) f is analytic but not necessarily a constant function
- (C) f is a constant function
- (D) $\lim_{z \rightarrow 0} f(z)$ exists

Q.No. 37 For a subset S of a topological space, let $\text{Int}(S)$ and \bar{S} denote the interior and closure of S , respectively. Then which of the following statements is TRUE?

- (A) If S is open, then $S = \text{Int}(\bar{S})$
- (B) If the boundary of S is empty, then S is open
- (C) If the boundary of S is empty, then S is not closed
- (D) If $\bar{S} \setminus S$ is a proper subset of the boundary of S , then S is open

Q.No. 38 Suppose $\mathfrak{T}_1, \mathfrak{T}_2$ and \mathfrak{T}_3 are the smallest topologies on \mathbb{R} containing S_1, S_2 and S_3 , respectively, where

$$S_1 = \left\{ \left(a, a + \frac{\pi}{n}\right) : a \in \mathbb{Q}, n \in \mathbb{N} \right\},$$

$$S_2 = \{ (a, b) : a < b, \quad a, b \in \mathbb{Q} \},$$

$$S_3 = \{ (a, b) : a < b, \quad a, b \in \mathbb{R} \}.$$

Then

- (A) $\mathfrak{T}_3 \supsetneq \mathfrak{T}_1$
- (B) $\mathfrak{T}_3 \supsetneq \mathfrak{T}_2$
- (C) $\mathfrak{T}_1 = \mathfrak{T}_2$

(D) $\mathfrak{S}_1 \supsetneq \mathfrak{S}_2$

Q.No. 39 Let $M = \begin{bmatrix} \alpha & 3 & 0 \\ \beta & 3 & 1 \\ 0 & 1 & 2 \end{bmatrix}$. Consider the following statements:

I: There exists a lower triangular matrix L such that $M = LL^t$, where L^t denotes transpose of L .

II: Gauss-Seidel method for $Mx = b$ ($b \in \mathbb{R}^3$) converges for any initial choice $x_0 \in \mathbb{R}^3$.

Then

- (A) I is not true when $\alpha > \frac{9}{2}$, $\beta = 3$
- (B) II is not true when $\alpha > \frac{9}{2}$, $\beta = -1$
- (C) II is not true when $\alpha = 4$, $\beta = \frac{3}{2}$
- (D) I is true when $\alpha = 5$, $\beta = 3$

Q.No. 40 Let I and J be the ideals generated by $\{5, \sqrt{10}\}$ and $\{4, \sqrt{10}\}$ in the ring $\mathbb{Z}[\sqrt{10}] = \{a + b\sqrt{10} \mid a, b \in \mathbb{Z}\}$, respectively. Then

- (A) both I and J are maximal ideals
- (B) I is a maximal ideal but J is not a prime ideal
- (C) I is not a maximal ideal but J is a prime ideal
- (D) neither I nor J is a maximal ideal

Q.No. 41 Suppose V is a finite dimensional vector space over \mathbb{R} . If W_1, W_2 and W_3 are subspaces of V , then which of the following statements is TRUE?

- (A) If $W_1 + W_2 + W_3 = V$ then $\text{span}(W_1 \cup W_2) \cup \text{span}(W_2 \cup W_3) \cup \text{span}(W_3 \cup W_1) = V$
- (B) If $W_1 \cap W_2 = \{0\}$ and $W_1 \cap W_3 = \{0\}$, then $W_1 \cap (W_2 + W_3) = \{0\}$
- (C) If $W_1 + W_2 = W_1 + W_3$, then $W_2 = W_3$
- (D) If $W_1 \neq V$, then $\text{span}(V \setminus W_1) = V$

Q.No. 42 Let $\alpha, \beta \in \mathbb{R}, \alpha \neq 0$. The system

$$\begin{aligned} x_1 - 2x_2 + \alpha x_3 &= 8 \\ x_1 - x_2 + x_4 &= \beta \\ x_1, x_2, x_3, x_4 &\geq 0 \end{aligned}$$

has NO basic feasible solution if

- (A) $\alpha < 0$, $\beta > 8$
- (B) $\alpha > 0$, $0 < \beta < 8$
- (C) $\alpha > 0$, $\beta < 0$
- (D) $\alpha < 0$, $\beta < 8$

Q.No. 43

Let $0 < p < 1$ and let

$$X = \left\{ f: \mathbb{R} \rightarrow \mathbb{R} \text{ is continuous and } \int_{\mathbb{R}} |f(x)|^p dx < \infty \right\}.$$

For $f \in X$, define

$$|f|_p = \left(\int_{\mathbb{R}} |f(x)|^p dx \right)^{\frac{1}{p}}.$$

Then

- (A) $|\cdot|_p$ defines a norm on X
- (B) $|f + g|_p \leq |f|_p + |g|_p$ for all $f, g \in X$
- (C) $|f + g|_p^p \leq |f|_p^p + |g|_p^p$ for all $f, g \in X$
- (D) if f_n converges to f pointwise on \mathbb{R} , then $\lim_{n \rightarrow \infty} |f_n|_p = |f|_p$

Q.No. 44 Suppose that ϕ_1 and ϕ_2 are linearly independent solutions of the differential equation

$$2x^2 y'' - (x + x^2) y' + (x^2 - 2) y = 0,$$

and $\phi_1(0) = 0$. Then the smallest positive integer n such that

$$\lim_{x \rightarrow 0} x^n \frac{\phi_2(x)}{\phi_1(x)} = 0$$

is _____

Q.No. 45 Suppose that $f(z) = \prod_{n=1}^{17} \left(z - \frac{\pi}{n} \right)$, $z \in \mathbb{C}$ and $\gamma(t) = e^{2it}$, $t \in [0, 2\pi]$. If

$$\int_{\gamma} \frac{f'(z)}{f(z)} dz = \alpha \pi i,$$

then the value of α is equal to _____

Q.No. 46 If $\gamma(t) = \frac{1}{2} e^{3\pi i t}$, $t \in [0, 2]$ and

$$\int_{\gamma} \frac{1}{z^2(e^z - 1)} dz = \beta \pi i,$$

then β is equal to _____ (correct up to one decimal place)

Q.No. 47 Let $K = \mathbb{Q}(\sqrt{3 + 2\sqrt{2}}, \omega)$, where ω is a primitive cube root of unity. Then the degree of extension of K over \mathbb{Q} is _____

Q.No. 48

Let $\alpha \in \mathbb{R}$. If $(3, 0, 0, \beta)$ is an optimal solution of the linear programming problem

$$\text{minimize } x_1 + x_2 + x_3 - \alpha x_4$$

subject to

$$2x_1 - x_2 + x_3 = 6$$

$$-x_1 + x_2 + x_4 = 3$$

$$x_1, x_2, x_3, x_4 \geq 0$$

then the maximum value of $\beta - \alpha$ is _____

Q.No. 49 Suppose that $T: \mathbb{R}^4 \rightarrow \mathbb{R}[x]$ is a linear transformation over \mathbb{R} satisfying

$$T(-1, 1, 1, 1) = x^2 + 2x^4, \quad T(1, 2, 3, 4) = 1 - x^2,$$

$$T(2, -1, -1, 0) = x^3 - x^4.$$

Then the coefficient of x^4 in $T(-3, 5, 6, 6)$ is _____

Q.No. 50 Let $\vec{F}(x, y, z) = (2x - 2y \cos x) \hat{i} + (2y - y^2 \sin x) \hat{j} + 4z \hat{k}$ and let S be the surface of the tetrahedron bounded by the planes

$$x = 0, y = 0, z = 0 \text{ and } x + y + z = 1.$$

If \hat{n} is the unit outward normal to the tetrahedron, then the value of

$$\iint_S \vec{F} \cdot \hat{n} \, dS$$

is _____ (rounded off to two decimal places)

Q.No. 51 Let $\vec{F} = (x + 2y)e^z \hat{i} + (ye^z + x^2) \hat{j} + y^2z \hat{k}$ and let S be the surface

$x^2 + y^2 + z = 1, z \geq 0$. If \hat{n} is a unit normal to S and

$$\left| \iint_S (\nabla \times \vec{F}) \cdot \hat{n} \, dS \right| = \alpha\pi.$$

Then α is equal to _____

Q.No. 52 Let G be a non-cyclic group of order 57. Then the number of elements of order 3 in G is _____

Q.No. 53 The coefficient of $(x - 1)^5$ in the Taylor expansion about $x = 1$ of the function

$$F(x) = \int_1^x \frac{\log_e t}{t-1} \, dt, \quad 0 < x < 2$$

is _____ (correct up to two decimal places)

Q.No. 54 Let $u(x, y)$ be the solution of the initial value problem

$$\frac{\partial u}{\partial x} + (\sqrt{u}) \frac{\partial u}{\partial y} = 0, \quad u(x, 0) = 1 + x^2.$$

Then the value of $u(0, 1)$ is _____ (rounded off to three decimal places)

Q.No. 55 The value of

$$\lim_{n \rightarrow \infty} \int_0^1 nx^n e^{x^2} dx$$

is _____ (rounded off to three decimal places)

Copyright : GATE 2020, IIT Delhi



GATE 2020

Graduate Aptitude Test in Engineering 2020

IIT Delhi
Organising Institute



[Home](#) [Information Brochure](#) [GATE International](#) [Pre Examination](#) [Important Dates](#) [FAQs](#) [Contact Us](#)

Answer Key - MA: Mathematics

Q.No.	Session	Que.Type	Sec. Name	Key	Marks
1	3	MCQ	GA	C	1
2	3	MCQ	GA	B	1
3	3	MCQ	GA	D	1
4	3	MCQ	GA	D	1
5	3	MCQ	GA	B	1
6	3	MCQ	GA	D	2
7	3	MCQ	GA	C	2
8	3	MCQ	GA	B	2
9	3	MCQ	GA	B	2
10	3	MCQ	GA	B	2
1	3	MCQ	MA	A	1
2	3	MCQ	MA	C	1
3	3	MCQ	MA	D	1
4	3	MCQ	MA	B	1
5	3	MCQ	MA	B	1
6	3	MCQ	MA	A or D	1
7	3	MCQ	MA	C	1
8	3	MCQ	MA	A	1
9	3	MCQ	MA	B	1
10	3	MCQ	MA	C	1
11	3	MCQ	MA	D	1
12	3	MCQ	MA	C	1
13	3	MCQ	MA	A	1
14	3	NAT	MA	1 to 1	1
15	3	NAT	MA	5 to 5	1
16	3	NAT	MA	80 to 80	1
17	3	NAT	MA	5 to 5	1
18	3	NAT	MA	5.5 to 5.5	1
19	3	NAT	MA	1.70 to 1.80	1
20	3	NAT	MA	36 to 36	1
21	3	NAT	MA	0.25 to 0.25	1
22	3	NAT	MA	3 to 3	1
23	3	NAT	MA	5 to 5	1
24	3	NAT	MA	121 to 121	1
25	3	NAT	MA	10 to 10	1
26	3	MCQ	MA	A	2
27	3	MCQ	MA	C	2
28	3	MCQ	MA	A	2
29	3	MCQ	MA	C	2
30	3	MCQ	MA	A	2
31	3	MCQ	MA	D	2
32	3	MCQ	MA	B	2
33	3	MCQ	MA	B	2

34	3	MCQ	MA	B	2
35	3	MCQ	MA	C	2
36	3	MCQ	MA	A	2
37	3	MCQ	MA	B	2
38	3	MCQ	MA	C	2
39	3	MCQ	MA	D	2
40	3	MCQ	MA	B	2
41	3	MCQ	MA	D	2
42	3	MCQ	MA	D	2
43	3	MCQ	MA	C	2
44	3	NAT	MA	3 to 3	2
45	3	NAT	MA	56 to 56	2
46	3	NAT	MA	0.5 to 0.5	2
47	3	NAT	MA	4 to 4	2
48	3	NAT	MA	7 to 7	2
49	3	NAT	MA	5 to 5	2
50	3	NAT	MA	1.30 to 1.40	2
51	3	NAT	MA	2 to 2	2
52	3	NAT	MA	38 to 38	2
53	3	NAT	MA	0.04 to 0.04	2
54	3	NAT	MA	1.610 to 1.625	2
55	3	NAT	MA	2.710 to 2.725	2

Copyright : GATE 2020, IIT Delhi

